

# The role of schools in the production of achievement

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## Abstract

What explains differences in pre-market factors? Three type of inputs are believed to determine the skills agents take to the labor market: ability, family inputs and school inputs. Therefore to answer the previous question it is crucial to understand first the importance of each of those inputs. The literature on the production of achievement has not been able to provide an estimation that can take the three factors into account simultaneously at the student level. This paper intends to fill this gap by providing an estimation of the production function of achievement where both types of investments (families and schools) are considered in a framework where the inputs are allowed to be correlated with the unobserved term, ability. I do that by applying Olley and Pakes' (1996) algorithm which accommodates for endogeneity problems in the choice of inputs for the production of achievement and by using parents' saving for their child postsecondary education to control for the unobserved component (i.e. ability to learn) in the production of skills. The estimates for the role of family inputs are in line to previous findings. Additionally, the estimates of school inputs show that they are also important for the formation of students' skills even after controlling for ability.

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# 1 Introduction

The literature on sources of inequality find that “pre-market” factors, skills individuals acquire before entering the labor market, explain most of income inequality across individuals and between groups of individuals. In that line, Neal and Johnson (1996) conclude that the observed wage gap between black and white students mostly disappears once we control for “pre-market” factors, measured by the Armed Forces Qualifying Test (AFQT). Likewise, Keane and Wolpin (1997, 2001) and Cameron and Heckman (1998) suggest that labor market outcomes are largely determined by skills acquired during the school-age period. More recently, Carneiro et. al. (2005) find that factors determined outside of the market play a major role in accounting for minority-majority wage differentials in modern labor markets. Hugget, Ventura and Yaron (2007) also conclude that differences in human capital at age 20 explain most of the variation both in lifetime utility and lifetime earnings.

But what explains those differences in “pre-market” factors? An answer to this question is important for policies aiming to provide equal opportunities in the labor market. This question becomes even more important as several studies (see for example Cunha and Heckman (2007a, 2007b), Currie and Duncan (1995), Blau and Currie (2006), Fryer and Levitt (2004)) document that test score gaps between blacks and whites widen with age. Therefore understanding how skills are acquired and evolve over time, i.e. their dynamics, and the importance of the three main inputs (ability, family inputs and school inputs) is very relevant. Even though many efforts have been made to understand how skills are produced at early stages of life, the existing literature has not been able to provide an estimation that can take these three factors into account simultaneously at the student level. This paper intends to fill this gap by providing an estimation of the production function of achievement where both types of investments (families and schools) are considered in a framework that accommodates for their relation with the unobserved term, ability. I achieve that by combining Olley and Pakes’ (1996) estimation strategy for production functions with a very suitable dataset, NELS:88, which provides information not only on home and school inputs, but also on how much parents save for their children’ postsecondary education. This saving decision helps identifying the third input of the production function: students’ ability to learn. What makes this saving measure informative is the fact that parents decide it at the same time they choose the inputs that will affect the observed test score (the current outcome), but those savings will affect the

future outcome, not the current outcome.

Todd and Wolpin (2003) address the problems in estimating the production function of achievement: *“Nonexperimental studies are based on observational data, where a reasonable assumption is that inputs into the education production process are subject to choices made by parents and schools. The fact that inputs are chosen purposefully would not necessarily pose a problem in estimating a production function for achievement if data on all relevant inputs as well as child endowments were observed; but, it does pose a problem when data on relevant inputs and endowments are missing. Thus, an important question ... is how to account for unobservable and for potential endogeneity of observed inputs in modeling the relationship between cognitive achievement and school and family inputs.”* (page F6). That is, when studying children’s performance on tests we would like to have information on all past and present family and school inputs and on the children’s ability. Unfortunately, such a dataset is not available and different estimation procedures have been proposed to deal with these data restrictions.

One line of the literature merges the National Longitudinal Survey of Youth of 1979 Children and Young adults (NLSY79-CS) with the Common Core Data (CCD). The NLSY79-CS provides reliable information about families’ characteristics and home investments in children, while the CCD includes school variables at the county level as proxies of the true school inputs students receive. Todd and Wolpin (2006) conclude, based on an out-of-sample root-mean square error (RMSE) criterion, that a value-added specification, i.e. an specification where current test scores are a function of past test scores and inputs, is the preferred specification. Using this specification, the authors find that differences in mothers’ ability (measured by AFQT) and home inputs explain large portions of test score gaps. In terms of the school characteristics, Todd and Wolpin find that their implied impact is very small compared to that of home inputs and mothers’ AFQT. Consequently, school inputs are not considered in the decomposition of the test score gap. Lui, Mroz and van der Klaauw (2006), using the same data, estimate a structural model of migration and maternal employment decision. Their main idea for the migration decision is that parents choose a place of residence in part because of employment opportunities and in part because of the characteristics of the schools in that district. Mothers make their employment decision knowing that their time has to be divided into how much to work in the market and how much to invest in her child. Using the

estimated equations for the residential location decision, the mother's employment choice and the child's outcome equation (a function of two endogenous inputs, maternal employment and school inputs), the authors study the effect of exogenously changing school characteristics and mothers' wages. Their finding is that once parental responses are taken into account, that is, after parents adjust their location and the mother's labor supply decision, policy changes have only minor impact on child test scores. The problem with this approach is that it uses school characteristics at the county level, not the true school input the child is receiving, while an important dispersion in school quality is observed within counties when school level data is considered.

Another line of the literature has focused on the unobserved component of the production function; i.e. ability, while keeping school inputs implicit. Cunha (2007) estimates a production function using factor analysis in nonlinear settings. He recovers the unobserved distribution of initial skills and that of ability (or heterogeneity at later ages). For the distribution of initial skills he uses characteristics at birth (weight and height), and for heterogeneity at later ages he considers some choices people make later in their lives (such as age at highest grade completed, the number of children they have by 2004, the frequency respondent consumes alcohol in 2004, probation by year 2004). Cunha concludes that the policy that subsidizes early and late childhood investments dominates the policy that reduces college tuition costs, providing evidence in favor of the existence of critical periods for investment in human capital. Cunha and Heckman (2007a, 2007b) provide additional estimates of the production function focusing in the substitutability/complementarity between cognitive and noncognitive<sup>1</sup> skills at both a point in time and across time. One salient conclusion is that noncognitive skills foster the formation of cognitive skills, but not vice versa. As in Cunha (2007) they find evidence of critical periods in investment. Additionally, they find evidence of selfproductivity, i.e. higher stocks of skills in one period create higher stocks of skills in the next period, and of dynamic complementarity, i.e. stocks of skills acquired in a previous period make current investments more productive. Although this approach tries to overcome the endogeneity between inputs and the unobservable, it does not take into account school inputs. If school inputs have a different impact from home inputs their conclusions might be misleading, especially when studying policies concerning school inputs such as the Perry

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<sup>1</sup>Cognitive skills always are referred to some measure of achievement, usually a test score, while noncognitive skills refer to "soft skills" such as motivation, persistence, time preference, and self control.

Preschool Program considered by Cunha and Heckman (2007a) .

In this paper I provide an estimation of the production function of achievement that attempts to overcome the aforementioned problems. To that end I propose an estimation strategy that takes into account not only the dynamics of the accumulation of human capital, but also the choice of whether or not to attend schools. This is achieved by borrowing Olley and Pakes' (1996) estimation algorithm and by using savings for postsecondary education to recover students' unobserved ability to learn<sup>2</sup>. I do this by using a dataset with student level information about family and school inputs (NELS:88). This is important because previous literature has either ignored school inputs or used county level variables, with much less variability. To the best of my knowledge this is the first paper using savings for postsecondary education to recover a measure of parents' knowledge about their children's ability at the moment they make their input decision. More importantly, this approach allows me to disentangle the effect of ability from the effect of previous test score on current test score (see section 2.2). This is the main reason why an IV approach is not useful in the present context. Because ability affects students' performance every period, it is embedded in the lag test score, and therefore any valid instrument will be also correlated with the lag test score and will not allow us to recover its coefficient in the production function of achievement. Identifying the effect of previous achievement on current achievement is important for analyzing the dynamics of educational policies .

The econometric strategy I use follows the algorithm suggested by Olley and Pakes to estimate the production function of firms, which has been widely used in the Industrial Organizational (IO) literature. The link between both problems is very clear. In the IO literature, when a researcher estimates the production function of an industry he faces two problems. A firm chooses their variable inputs (labor) knowing how productive it is, measured, for example, by its managerial ability. But this measure is not available to the econometrician and introduces endogeneity problems. Moreover, not all potential firms decide to enter the market, but only those that find it profitable to do so. This generates a selection problem. In the current framework similar problems are present. Parents choose how much to invest in their child (home inputs) knowing their child's ability. However, the econometrician does

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<sup>2</sup>Cooley (2007) uses a similar invertibility condition to identify students' ability. She assumes that the portion of leisure time spent reading for fun is a function of students' ability . She then inverts this function to recover students' ability.

not observe the child's ability, which introduces endogeneity problems. Additionally, some students decide to dropout from school, and so they do not receive school inputs. This introduces a selection problem, as only students that expect a profitable return from school will attend. The idea of the identification strategy is the following: Every period parents observe their child's characteristics as well as other house-related characteristics (such as family income, parents' education) and decide whether to send the child to school, how many inputs to invest in that period and whether or not to save for the child's postsecondary education (postsecondary education being significantly more expensive than elementary or high school). This parental saving decision is used to back up the ability, or unobserved, component. Therefore the identification strategy relies on the assumption that, conditional upon all the other observable variables affecting the saving decision, there exists a one-to-one mapping between savings and the unobserved term. Section 2.2 provides evidence supporting this assumption. Another potential problem of the identification strategy is whether we are capturing "ability to learn". To study that in Section 4.3 I test for the presence of measurement error and a preference shifter, a students' fixed effect, in the saving function. I do that by incorporating the identification strategy for polynomials errors-in-variable model (Hausman, Newey, Ichimura and Powell (1991) and Hausman, Newey and Powell (1995)) to the standard Olley and Pakes' algorithm.

I use the estimates of the production function of achievement to perform some counterfactual exercises. Following the literature, I focus on the black-white test score gap. In particular, I do an out of the sample exercise where blacks receive the average inputs that whites in the sample are receiving. As opposed to what was found previously in the literature, the results suggest that schools are important in helping blacks to catch up to their white counterparts. Moreover, if inputs are altered only in 12th grade, school inputs turn out to have a higher impact on students' achievement than home inputs do. A policy that gives inputs in both 8th and 12th grade is found to be more effective than intervening only in 12th grade, a result that is consistent with the findings in Cunha (2007) . I also test for the presence of self productivity by studying how much of the gap is due to differences in skills students bring to 8th grade. The results show that initial skills are very important, supporting previous evidence that early investments are more productive than later investments.

The order of the paper is the following: Section 2 starts by pointing out the potential

estimation problems by using OLS and presents the proposed estimation strategy. Section 3 describes the data and the variables to be used in the estimation and Section 4 presents the empirical results. Finally, section 5 concludes.

## 2 A proposed framework to overcome estimation problems

The goal is to get consistent estimates of the following production function of achievement (ACH):

$$h_t^* = f_t( \underbrace{h_{t-1}}_{\text{previous ACH}}, \underbrace{x_t}_{\text{home inputs}}, \underbrace{e_t}_{\text{school inputs}}, \underbrace{H}_{\text{parents' HC (education)}}, \underbrace{\eta_t}_{\text{ability to learn}} ) \quad (1)$$

In order to illustrate the estimation problems faced when trying to estimate the  $f_t(\cdot)$  function, consider the value added specification.<sup>3</sup> That is, assume that the production function of achievement is:

$$h_t = \beta_0 + \beta_1 x_t + \beta_2 e_t + \beta_3 H_t + \beta_4 h_{t-1} + \eta_t + \varepsilon_t \quad (2)$$

where

$$h_t = h_t^* + \varepsilon_t$$

i.e.  $\varepsilon$  allows for classical measurement error.

If we want to estimate the production function of achievement a natural starting point is Ordinary Least Squares (OLS). In the first subsection I describe the problems we face if we choose that strategy. Then the econometric strategy used in this paper is explained.

### 2.1 Basic problems of OLS estimates

To illustrate potential biases suppose that cognitive skills are produced according to the following technology:

$$h_t = \gamma_0 + \gamma_1(I_t) + \gamma_2 h_{t-1} + \underbrace{\eta_t + \varepsilon_t}_{\mu_t} \quad (3)$$

where  $I$  accounts for all inputs. The main problem of estimating such a technology by OLS is that as econometricians we do not observe students' ability. Thus the error term becomes

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<sup>3</sup>This specification was first suggested by Hanushek (1986) and has been widely used in the education literature since then. Todd and Wolpin (2006) find, based on a RMSE criterion, the value added specification to be preferred over different reduced form specifications (contemporaneous, cumulative, child fixed effect and sibling fixed effect) for the estimation of the production function.

$\mu_t = \eta_t + \varepsilon_t$ . In this case the OLS estimates are:

$$\hat{\gamma}_1 = \gamma_1 + \underbrace{\frac{\hat{\sigma}_{h,h}\hat{\sigma}_{I,\eta}}{\hat{\sigma}_{h,h}\hat{\sigma}_{I,I} - \hat{\sigma}_{I,h}^2}}_{\text{simultaneity bias}} - \underbrace{\frac{\hat{\sigma}_{h,I}\hat{\sigma}_{h,\eta}}{\hat{\sigma}_{h,h}\hat{\sigma}_{I,I} - \hat{\sigma}_{I,h}^2}}_{\text{selection bias}}$$

$$\hat{\gamma}_2 = \gamma_2 + \underbrace{\frac{\hat{\sigma}_{I,I}\hat{\sigma}_{h,\eta}}{\hat{\sigma}_{h,h}\hat{\sigma}_{I,I} - \hat{\sigma}_{I,h}^2}}_{\text{selection bias}} - \underbrace{\frac{\hat{\sigma}_{I,h}\hat{\sigma}_{I,\eta}}{\hat{\sigma}_{h,h}\hat{\sigma}_{I,I} - \hat{\sigma}_{I,h}^2}}_{\text{simultaneity bias}}$$

where  $\hat{\sigma}_{a,b}$  denote the sample covariance between  $a$  and  $b$ . This introduces two types of biases.

- Endogeneity bias: following the arguments in Todd and Wolpin (2003) any economic model of optimizing behavior predicts that the amount of resources allocated to a child will be responsive to the parent's perception of a child's ability. That is, parents choose inputs once they observe their child's ability, so we should expect  $\sigma_{I,\eta}$  to be different from zero. It could be either positive or negative. On the one hand, it could happen that parents observing that their child is of high ability expect a higher return to their investment and so invest more in him. In this case it would exist a positive correlation between children's ability to learn and the amount of inputs. On the other it could be that parents who observe that their child is of low ability try to compensate this by investing more inputs. This type of behavior would induce a negative sample correlation between student's ability to learn and the level of inputs.
- Selection bias: it will exist if only those children for whom is profitable to attend school do not drop out from them. Therefore, the distribution of unobserved ability to learn in the sample is not the unconditional distribution, but the truncated distribution. If in this context children of higher ability are sent to school under lower realization of previous test scores, i.e. when they do bad in school, because they can catch up later, the truncation point of the ability distribution will be negatively correlated with the previous test score. Hence the sample average of ability will be decreasing in previous test score.

To overcome the two types of biases we need a framework which determines both the information available when inputs decisions are made and an exit rule from schools. The proposed econometric strategy deals with both problems.

## 2.2 Econometric Strategy

The baseline econometric strategy is analogous to Olley and Pakes (1996). I assume that every school year parents observe the stock of human capital of their child, the child's ability to learn, and other household characteristics such as their family income. I assume as well that ability to learn follows a first order Markov process. If the child is old enough so that school attendance is no longer compulsory parents can decide, given the information they have, whether the child will go to school or dropout. After high school the child might attend a postsecondary institution, and parents can start saving for their child's postsecondary education in advance. The basic idea of the identification strategy is that parents make a saving decision to afford postsecondary education while their child is at middle and high school. They make this decision based on their family income, their stock of savings, the child's achievement and *the child's ability*<sup>4</sup>, i.e. :

$$s_t = s_t(H, \eta_t, S_{t-1}, h_{t-1})$$

In turn, the child's ability will determine the likelihood of attending college, whether he/she will get financial aid and which type of college he/she will be able to attend. Observing savings for postsecondary education allows me to recover the distribution of ability, as ability affects savings but savings do not affect the child's level of achievement in the current period.

Conditional on the other set of variables, we can invert this function to back up  $\eta_t$ :

$$\eta_t = f_t(H, S_t, h_{t-1}) \tag{4}$$

Note that to be able to invert this function I rely on the assumption that, conditional on the other set of variables, there exists a continuous and monotonic choice of savings based on the child's ability. Under its assumptions the OP algorithm, can be summarized in the next three steps:

- Once we replace the proxy for students' ability to learn (equation (4)) in the production function of achievement (equation (2)) the endogeneity problem disappears and we can recover the coefficients on contemporary inputs, i.e. those inputs chosen after parents observe shocks in the current period. Because the stock of human capital that children bring to the period affects the saving decision, we are not able to separate its effect

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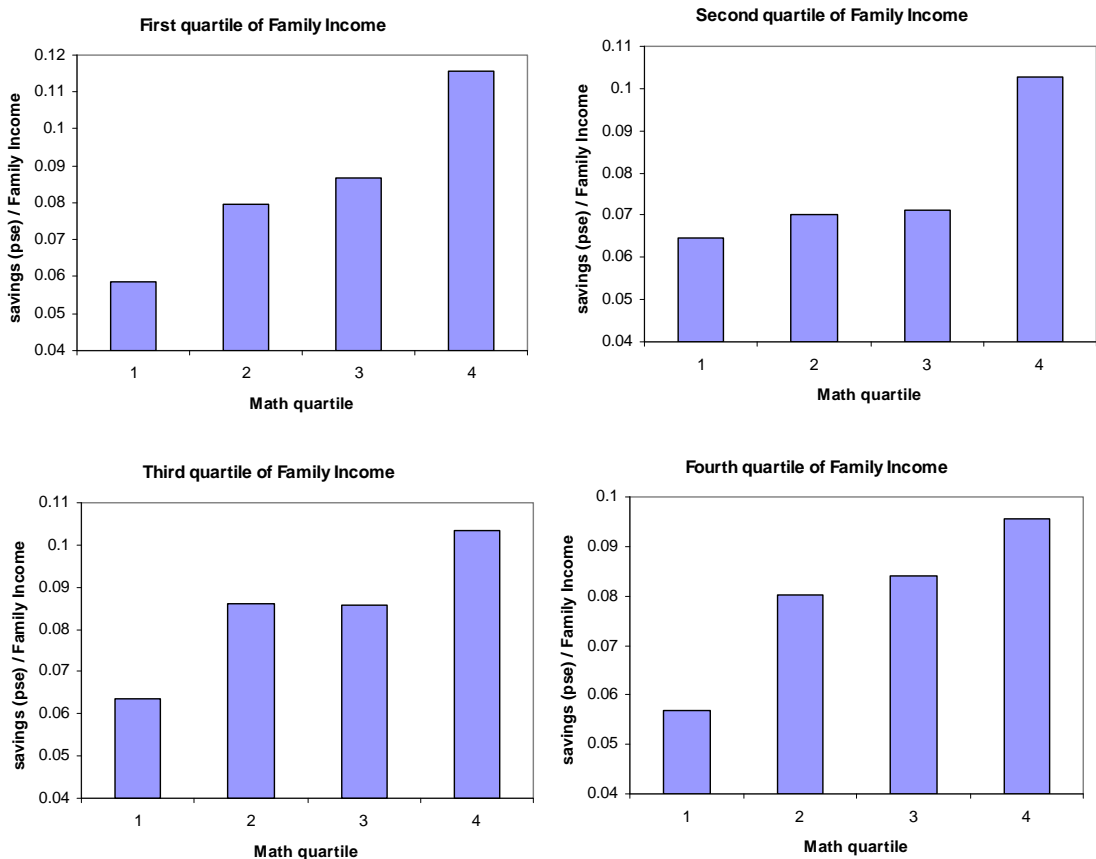
<sup>4</sup>This result can be obtained from a simple overlapping generation model where parents care about the wellbeing of all their dynasty.

on savings from its effect on the acquisition of more human capital. The rest of the algorithm helps disentangling those two effects.

- In order to be able to identify the effect of the lag test score we need to estimate first the expectation of the unobservable. For that we need to deal with selection, i.e. estimate the probability that a certain observation that is in the data in period  $t$  remains alive in period  $t + 1$ . The reason is that in the sample we only observe school inputs for those students that find profitable to attend school, consequently we can only recover the mean of the truncated distribution of ability to learn. Therefore we need an estimate of that truncation point.
- With the estimates of contemporary inputs plus a measure of the survival probability, we can recover the effect of the lag test score on the production of achievement through a nonlinear estimation.

As I mentioned before, the algorithm relies on the assumption that there exists a continuous and monotonic choice of savings based on the child's ability. Two cases might break this monotonicity assumption: if savings depend only on family income or if savings depend only on parents' expectations about financial aid or some other way their children might find to face the cost of postsecondary education.

In the first case, if savings depend only on family income, then we should expect richer families to save more independently of their children's level of achievement. If this is the case, conditional on family income there will be no relation between savings and achievement. Figure 1 shows the relation between students performance in math test score and savings for each quartile of family income. It can be observed that parents of children that do better tend to save more for their child's postsecondary education within each income quartile. Thus, there is evidence that conditional on family income there exists a relation between the saving decision and students achievement.



The second case is more complex and requires the consideration of more variables. If parents of high ability students think their children will be able to get enough merit-based financial aid to face all his/her postsecondary expenses, it might not be optimal to save and reduce current consumption. The child could afford the expenses anyway and parents could increase lifetime utility by increasing current consumption. The same logic could apply for need-based financial aid, i.e. assigned based on family income. If this was the case we could observe a hump shaped relation between savings and ability breaking the monotonicity relation and so the identification strategy. But this argument is based on the assumption that the education decision depends only on the cost. However there could also be a quality dimension on that decision. Therefore, understanding how financial aid works and how it affects net price of attendance<sup>5</sup> at different postsecondary institutions is of vital importance to study whether the identification assumption is correct.

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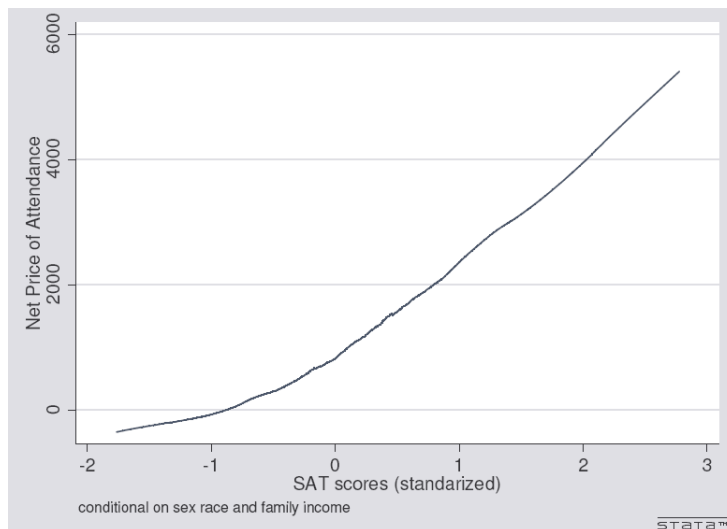
<sup>5</sup>Net price of attendance is usually defined as tuition plus room and board minus financial aid, i.e. what the student and/or family must cover after financial aid.

There are three sources of financial aid for students attending postsecondary institutions. The first, and most important in terms of budget, are financial need-based governmental sources (such as the Pell Grant, Perkin Loans, Stafford subsidized loans and the Supplemental Educational Opportunity Grant (SEOG)). The second are governmental loans that are not need based, as the Stafford unsubsidized loans and the PLUS loans, but those are not commonly used in practice. Finally, colleges and universities offer their own grants which in most cases are merit based-in that they are assigned to students that attained a certain GPA in high school (usually above 3.0) or satisfy some other academic criteria.

An additional important aspect is that financial aid does not usually cover all postsecondary expenses. Parents should expect to pay at least half to two-thirds of their children's college costs through a combination of savings, current income, and loans. Gift aid from the government, colleges and universities, and private scholarships account for only about a third of total college costs. According to data from the Education Department for the 1995-96 academic year Lee (2001) finds that 91.9% of students attending postsecondary schools with tuition and fees above \$12,000 receive some direct financial contribution from their parents. Among those students attending institutions with tuitions and fees below \$12,000 this percentage was 79.6% in public research universities and 70.8% for other institutions. In sum, for most students the net price of attendance is positive.

Therefore the empirical evidence suggests that: financial aid is based on observables that we take care of in our estimation, and for most of the students it does not cover all of their postsecondary education expenses. However, this argument does not rule out the existence of a hump shaped relation between ability and cost of postsecondary education. On one extreme of the distribution we could have students from economically disadvantage families getting financial aid and on the other extreme high ability students getting it. This could imply that only students from the center of the achievement distribution, who would not qualify for neither need based nor merit based financial aid, would face higher costs. But this argument does not take into account other aspects that parents might take into account when choosing the postsecondary institutions for their children as for example the quality dimension of postsecondary education. If postsecondary costs are related to the quality of the institution and if the return to schooling depends on this quality, the previous argument does not need to hold. To study the relation between a measure of students' ability and the cost

of postsecondary education, I do a nonparametric regression between students' standardized composite SAT score and the actual net price of attendance they face for the students in the NELS88 sample. Figure 2 shows the result. The relation between SAT and net price of attendance is monotonically increasing, giving us evidence that there are some other aspects more than price affecting the choice of the postsecondary institution. The next subsections explain in more detail each of the algorithm's steps.



### 2.2.1 First Stage

Replacing  $\eta_t = f_t(H, s_t, h_{t-1})$  in the production function gives:

$$\begin{aligned}
 h_t &= \beta_0 + \beta_1 x + \beta_2 e_t + \beta_3 Y_t + \underbrace{\beta_4 h_{t-1} + f(H, S_t, h_{t-1})}_{\phi(H, S_t, h_{t-1})} + \varepsilon_t \\
 &= \beta_1 x_t + \beta_2 e_t + \beta_3 Y_t + \phi(H, S_t, h_{t-1}) + \varepsilon_t
 \end{aligned} \tag{5}$$

where  $Y_t$  accounts for all the control variables.

The first stage involves estimating (5) semiparametrically using a fourth order polynomial for  $\phi(\cdot)$ , i.e. treating  $f(\cdot)$  non-parametrically. As is noted by Akerberg et al. (2006) treating  $f(\cdot)$  nonparametrically has important advantages. The saving function might be a complicated function that depends on the primitives of a model and might be the solution of a dynamic optimization problem, the OP method allows us to avoid both the necessity of specifying the primitives of such a model and the burden of solving it numerically.

Note that because we are able to completely proxy for  $\eta_t$  the residual in (5) represents factors that are not observed by parents when making their inputs decisions. Therefore we

can get consistent estimates of  $\beta_1$ ,  $\beta_2$  and  $\beta_3$ . However, the non-parametric treatment of  $f(\cdot)$  does not allow to separate the effect of  $h_{t-1}$  on the production of current human capital from its effect on the saving decision.

### 2.2.2 Second Stage

The second stage let us get the intermediate estimates needed to back up the coefficient on lag test score. Note that from the estimates in the first stage we get:

$$\widehat{\eta}_t = \widehat{\phi}(H, S_t, h_{t-1}) - \beta_0 - \beta_4 h_{t-1} \quad (6)$$

that is, given a particular set of parameters  $(\beta_0, \beta_4)$  we can have an estimate of  $\eta_t$ .

Consider the expectation of human capital net of variable inputs in  $t + 1$  conditional on the information at the beginning of the period and not dropping from school:

$$\begin{aligned} & E \left[ h_{t+1} - \widehat{\beta}_1 x_{t+1} - \widehat{\beta}_2 e_{t+1} - \beta_3 \widehat{Y}_{t+1} / \eta_t, \chi_{t+1} = 1 \right] \\ &= \beta_0 + \beta_4 h_t + E \left[ \eta_{t+1} / \eta_t, \chi_{t+1} = 1 \right] \\ &= \beta_0 + \beta_4 h_t + E \left[ \eta_{t+1} / \eta_t, \eta_{t+1} \geq \underline{\eta}_{t+1}(H, S_t, h_t) \right] \\ &= \beta_0 + \beta_4 h_t + g(\eta_t, \underline{\eta}_{t+1}) \end{aligned} \quad (7)$$

where  $g(\eta_t, \underline{\eta}_{t+1}) = \int_{\underline{\eta}_{t+1}} \eta_{t+1} \frac{F(d\eta_{t+1}/\eta_t)}{\int_{\underline{\eta}_{t+1}} F(d\eta_{t+1}/\eta_t)}$ . To go from the second to the third line we

assume that the decision to not drop out from school depends on the child's ability to learn. Students above a certain threshold will continue in school. I assume that this threshold depends on his stock of achievement, the household characteristics, and the level of savings. All these variables will affect the probability of attending a postsecondary institution and therefore the probability of remaining in school.

In order to control for the selection, we need a measure of both:  $\eta_t, \underline{\eta}_{t+1}$ . This is an important difference between the OP algorithm and the standard propensity score literature as in the later only a measure the threshold value is needed.

We can get a measure of  $\eta_t$  from (6), but do not have a measure for  $\underline{\eta}_{t+1}$ . What the OP algorithm suggests is to use the data on observed exit to control for  $\underline{\eta}_{t+1}$ . Given the previous assumptions, we can write the probability of not dropping out from school in period  $t + 1$

conditional on the information available in period  $t$  as:

$$\begin{aligned}
& \Pr\left(\chi_{t+1} = 1/\eta_t, \underline{\eta}_{t+1}(H, S_t, h_t)\right) \\
&= \Pr\left(\eta_{t+1} \geq \underline{\eta}_{t+1}(H, S_t, h_t)/\eta_t, \underline{\eta}_{t+1}(H, S_t, h_t)\right) \\
&= p_t\left(\eta_t, \underline{\eta}_{t+1}(H, S_t, h_t)\right) = P_t
\end{aligned} \tag{8}$$

We can estimate (9) non-parametrically, using a fourth order polynomial in  $(H, S_t, h_t)$  as the latent index. I assume that the *i.i.d* shock received every period to the level of ability to learn follows a normal distribution. This implies that the probability of not dropping out from school follows a normal distribution as well.

Once we have an estimate for  $P_t$ , we can invert  $\widehat{P}_t$  to get a measure of  $\underline{\eta}_{t+1}$ , i.e.  $\underline{\eta}_{t+1}(\widehat{P}_t, \eta_t)$ . The only condition we need for that inversion to be possible is that the density of  $\eta_{t+1}$  given  $\eta_t$  is positive in an area around  $\underline{\eta}_{t+1}(H, S_t, h_t)$ .

### 2.2.3 Third stage

Substituting  $\widehat{P}_t$  and  $\widehat{\phi}$  in the production function we can get consistent estimates of the effect of lag test score:

$$\begin{aligned}
& h_{t+1} - \widehat{\beta}_1 x_{t+1} - \widehat{\beta}_2 e_{t+1} - \beta_3 \widehat{Y}_{t+1} \\
&= \beta_0 + \beta_4 h_t + \eta_{t+1} + \varepsilon_t \\
&= \beta_0 + \beta_4 h_t + g(\eta_t, \underline{\eta}_{t+1}) + \varsigma_t + \varepsilon_t \\
&= \beta_0 + \beta_4 h_t + g\left(\widehat{\phi} - \beta_0 - \beta_4 h_{t-1}, p_t^{-1}\left(\widehat{\phi} - \beta_0 - \beta_4 h_{t-1}, P_t\right)\right) + \varsigma_t + \varepsilon_t
\end{aligned}$$

Basically, this is a similar estimation as in the first stage where we use a fourth order polynomial to approximate  $g()$ , and estimate it by NNLS. Note that because of the approximation for  $g()$   $\beta_0$  cannot be identified. The identification of  $\beta_4$  comes from comparing students with the same  $\eta_t$  and  $P_t$  but different  $h_{t-1}$ .

## 3 Data

NELS:88 is a nationally representative sample of eighth-graders that were first surveyed in the spring of 1988. The original sample employed a two-stage sampling design, selecting first a sample of schools and then a sample of students within these schools. In the first stage the sampling procedure set the probabilities of selection proportional to the estimated

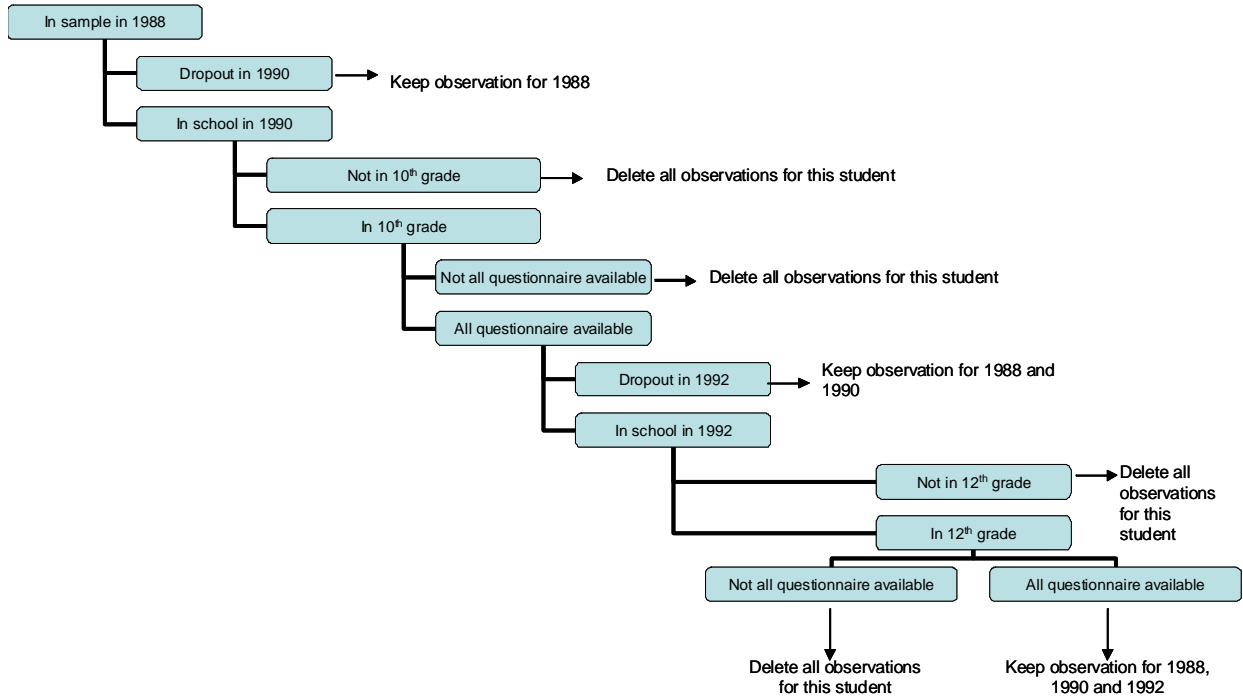
enrollment of eighth grade students. In the second stage 26 students were selected from each of those schools, 24 randomly and the other two among hispanic and Asian Islander students. Along with the student survey, NELS:88 included surveys of parents, teachers, and school administrators. A sample of these respondents were resurveyed through four follow-ups in 1990, 1992, 1994 an 2000. Consequently, NELS:88 represents an integrated system of data that tracked students from middle school through secondary and postsecondary education, labor market experiences, and marriage and family formation.(See Appendix C for more details about the survey’s sample and characteristics of each of the five collection years).

**Sample** From the 12,144 individuals in the NELS:88/2000 sample, I exclude those students that in 1988 belong to the “hearing impaired” sample, those students whose either their parent, teacher or school administrator did not return the questionnaire, and those students with missing test scores.

In 1990 these students can be divided into three groups. Those students that in 1990 dropout from school, only their 8th grade observation was kept in the sample. Among those students attending school in 1990, if the student was attending a different grade (that is, not in 10th grade) his complete history was deleted. If the student was in 10th grade and his teacher and school administrator answer the questionnaire I keep him in the sample. If any of these questionnaires are not available, his complete history was deleted.

I repeat the same procedure for the 1992 data. If the student dropout the observations while in school are kept in the data. For those in school, if the student was attending a grade different from 12th grade, all his observations are deleted from the sample. If the student is attending 12th grade, but either his parents, school administrator or teacher did not completed the questionnaire, all the observations for that student are deleted. Finally, students in 12th grade that had all relevant questionnaires completed are in the sample.

The following figure summarizes how I construct the sample:



The sample resulted in 6,293 students with answers for 1988. In the following years the sample shrinks due to dropouts. Consequently, the final sample is an unbalanced panel of students from 1988 to 1992.

**Achievement Measures** I use the percentile in the math test score distribution as a measure of students' achievement. All students in the sample took the same test provided by the Education Department Table 1 in Appendix A shows mean values of the math percentile test score in different school grades. Previous literature has focused in both math and read test scores finding qualitatively similar results with both types of tests. Because only the math teacher can be observed across different grades in school, all the analysis is based on the math test score. The descriptive statistics in Table 1 are in line with other datasets, the gap between whites and blacks is important and it is increasing over students life. In 8th grade, the average black student tend to perform in the third decile while the average white student is in percentile 52. At the end of the high-school period, the average white increase one percentile, i.e. it performs in percentile 53, while the average black was in the same

percentile as in 8th grade.

**Home inputs** NELS:88 includes a large set of questions related to families activities that might foster or discourage a students' test scores. Table 1 present some of the measures used in the empirical analysis by race. All the measures show that whites are more likely to receive home inputs that foster achievement than blacks. For example, black children tend to read outside school on average 0.3 hours less than whites in 8th grade, increasing the difference to half an hour by 12th grade. Blacks tend to watch on average more hours of tv than whites. While attending 8th grade a higher proportion of white children are sent to classes outside school (music, language, art) than whites, although this difference seems to narrow over time.

**School inputs** There are two types of school variables in NELS:88. One set of variables are observed at the school level, while the other correspond directly to the class level and are answered by the teacher. Table 1 shows the average value for some of these variables. As in the case of home inputs, there are important differences across race. Black students attend on average schools with worst characteristics to foster their human capital accumulation than white students. For example, blacks are on average in classes with almost a double of students receiving remedial classes than their whites counterparts (12.21% versus 5.38%). On average blacks are also in class whether the teacher spends a higher proportion of the class time just maintaining the order. Both groups seems to have teachers with similar characteristics, in terms of wages, experience and certification.

**Parents characteristics** One advantage of NELS:88 is that it provides information on both parents, mothers and fathers. Table 1 shows the proportion of parents with different years of education. Only 30% of black fathers attain some college or more, while almost 70% of white fathers do. Among mothers differences are important though not as high as with fathers. Having both parents' education is important to identify the home environment of the child. This seems important as at least in this sample there is evidence that mothers' education is not always the same as fathers' education (see Table 2, Appendix A). For example, within children whose mothers just completed high school, only 37% of the fathers had just completed high school, while 17% attended some college, 12% finished college and 34% are high school dropouts. Similar differences are observed for mothers with other schooling levels.

**Savings for postsecondary education** Savings parents make for postsecondary education are observed in every round of the survey where parents are surveyed. First parents are

asked whether they have done anything to have some money for they child’s education after high school. For those that answer yes, they are asked how much money they had set aside. Table 1 shows that although there are big differences by race, the average saving to family income ratio is similar across races. In the empirical analysis, this differences jointly with other family and child’s characteristics are going to give the identification for heterogeneity across kids.

## 4 Empirical Results

This section presents the estimates for the production function of achievement using the OP algorithm described in section 2.2. Two additional controls will be added to the ability function. The first one is race. Equation (4) assumes that there are not systematic differences in savings for postsecondary education across races while the empirical evidence suggests that it might not be the case, see for example Oliver and Shapiro (2006). I will control equation (4) for race to take care of this potential effect. Equation (4), assumes also that there are not gender differences. However, there is evidence that girls perform relatively below boys in math test scores (see for example Todd and Wolpin (2006)). Without taking into account gender differences and given that all the analysis is based in math test scores, I might underestimate the “ability to learn” of girls and this difference would be captured by the sex coefficient. Therefore I will control equation (4) by gender as well.

I present first the estimates for a value added production function and compared them with the standard OLS estimates for the same function. Then the estimates of a technology that allows for dynamic complementarity/substitutability are presented.

In Section 4.2 I use these estimates to perform some counterfactual exercises. Following the literature, most of the counterfactual exercises focus on the black-white test achievement gap. In particular, I study how the actual gap would change by exogenously altering the inputs a group of students receive. Finally Section 4.3 presents robustness analysis for the assumption that savings for postsecondary education is a good proxy for students’ ability to learn.

## 4.1 Estimates of the Production Function of Achievement

Table 3 presents the estimates for the production function under alternative specifications. The first column presents the estimates using OLS. Both home and school inputs are statistically significant for the production of achievement. The coefficient in the lag test score is statistically significant, positive and less than one. This result is in line previous literature. For example Currier and Thomas (2000) find that the effect of Head Start tend to fade out over time when not followed up by later investments.

The second column shows the estimates when the OP algorithm is used. The most important change with respect to the OLS estimates is in the effect of the lag test score, with its coefficient increasing in more than eight standard deviations. This result is in line with the standard predictions in the IO literature. Parents of children with larger stocks of human capital,  $h_{t-1}$ , should expect future higher returns for any level of their kid's ability to learn, hence they will choose to send their children to school under lower realizations of their ability. Consequently, we should expect the truncation point of students' ability to learn to be decreasing in  $h_{t-1}$  and if the production function of achievement is increasing in  $h_{t-1}$  this would imply a negative bias in the OLS estimate of its coefficient. (REWRITE CAMBIAR ORACION DE IO PREDICTION)

For the home and school inputs their coefficients are jointly statistically different under the OP estimations and the OLS estimation. Under the null hypothesis that they are equal, we get a  $\chi^2$  of 74.97 with a extremely low p-value. As was mentioned in section 2.1, a priory the bias from the OLS estimates in the home and school inputs could go either way depending on whether the substitution or wealth effect dominates. In this sample there is evidence that the substitution effect dominates as in most cases the impact of individual inputs goes down once we get rid of the endogeneity problem. (MIRARLO BIEN, IT SEEMS NOT TO BE ANYMORE) We also observe that the change in the school inputs is smaller than in the home inputs. This finding goes in line with the fact that when choosing a location of where to live or even to which school send their child parents can only choose an average "school quality" as parents are not in the classroom everyday. Instead, parents can choose their home inputs everyday and they can adjust them directly more easily. This would predict that home inputs have a higher correlation with students' ability to learn than school inputs explaining the lower bias of the OLS estimates.

In line with previous results in the literature there is evidence of sensitive periods. In this sense, the return of reading an extra hour decreases by 90% from 8th grade to 12th grade and it is not significant in the last case. In terms of the school inputs, the effect of the proportion of time that teachers use just to maintain the order of the class decreases by 34%.

Table 4 presents the estimates of a technology that allows for dynamic complementarity/substitutability in the production of skills. In particular, I estimate the following production function:

$$h_t = \beta_0 + \beta_1 x_t + \beta_2 e_t + \beta_3 Y_t + \beta_4 h_{t-1} + \gamma h_{t-1} (\beta_1 x_t + \beta_2 e_t) + \eta_t + \varepsilon_t \quad (9)$$

Note that in order to make the estimation more tractable all the inputs are compacted in an index, where each input's weight is their contribution to the production of achievement. This joint effect can be identified in the first stage of the algorithm, estimating this stage through NNLS, because current period inputs do not enter in the fourth order polynomial used to approximate the unobservable component.

The estimates show that the effect of skills in previous period changes significantly. Now  $\beta_4$  is smaller and  $\gamma$  is positive and significant. From equation (9):

$$\frac{\partial h_t}{\partial h_{t-1}} = \beta_4 + \gamma(\beta_1 x_t + \beta_2 e_t) \quad (10)$$

that is if investments are not followed by subsequent investments achievement tends to fade out more rapidly. There is also strong evidence for dynamic complementarity, the return to current investment is 1.28 times higher the higher the stock of skills acquired in previous periods.

## 4.2 Accounting Exercise

There exists a growing literature interested in understand the production of skills because they are important determinants of labor market outcomes. To understand the effect of different inputs, in this section I use the estimates from table 3 to study the impact of exogenously altering different types of inputs on students' achievement. Table 5 shows how the predicted black-gap would change under different scenarios. The first exercise shows the test score gap if black students would receive the average inputs whites receive in both 8th and 12 grade. The estimated impact turns out to be quite high, and in line to previous literature, when the OLS specifications are used. Home inputs would reduce the achievement gap by 16.9% while

equalizing school inputs would do it in 12.5%. When endogeneity and selection are taken into account, the impact of both home and school fall. Equalizing home inputs would close the gap by 13.1%. When instead blacks receive the average school inputs of whites, the predicted black-white test score gap decreases by 9.2%.

The second exercise is a “late remediation policy” where blacks receive the average inputs of whites only in 12th grade. The effect of both types of inputs in closing the gap decrease. However, in this case school inputs appear to be more effective. School inputs would reduce the gap by 5.7% while home inputs would do it by 4.7%. Several conclusions can be taken from this decomposition. First, school inputs matter, and they seem to be more important in fostering skills in high school. Cunha and Heckman (2007a, 2007b) find that at later ages investment are more effective over noncognitive skills and in turn this foster the accumulation of cognitive skills. Under this interpretation, it could be that schools are better at dealing with behavioral problems of teens than parents do, consequently through this channel they have a higher impact on students’ tests performance.

The estimates of the production function show that the lag test score is an important input. One important limitation of NELS:88 is that all the inputs information begins in 8th grade, when already many things had already occurred in children’s life. To see how much of the gap is due to these differences in skills at the beginning of 8th grade, I calculate predicted tests scores using the estimated parameters and giving every student the maximum initial test score observed in the sample. In this case 19.3% of the gap would be closed, implying that initial conditions are important for future performance. This result is also in line with previous findings in the literature which suggest that early investments are more productive than investment in latter ages.

### **4.3 Robustness: Estimation problems when savings is a poor proxy of unobserved ability to learn**

In order to estimate the contribution of home and school inputs to the production of achievement I suggest that:  $s_{it} = f(\eta_{it}, controls)$ , and assumed that this is the true function generating savings. In a more general set up, it could be that  $s_{it} = f(\eta_{it}, controls, \zeta_{it})$ , where  $\zeta_{it}$  is an additional, unobserved for the econometrician, component. For example  $\zeta_{it}$  could be measurement error. Alternatively, we could think that  $\zeta_{it}$  is a variable that affects the true savings function, like parents’ generosity towards their children. In this section I study

whether the inclusion of such a variable could bias the results and how I could solve this issue.

To derive the estimation problems we would face assume the production function of achievement is governed by the following technology:

$$h_{it} = \gamma_0 + \gamma_1 I_{it} + \nu_{it} \quad (11)$$

where  $\nu_{it} = \eta_{it} + \varepsilon_{it}$ , and where  $\eta_{it}$  is ability to learn and  $\varepsilon_{it}$  represents some idiosyncratic shock to the production of achievement or just classical measurement error in test scores. Without loss of generality, assume both components have mean zero. As mentioned in Section 2.1, any economic model of optimizing behavior would predict that the amount of resources allocated to a child will be responsive to the parent's perception of a child's ability, that is  $cov(I_{it}, \eta_{it}) \neq 0$ . To simplify the analysis assume that  $cov(I_{it}, \varepsilon_{it}) = 0$ .

In order to be illustrative lets keep aside the control variables considered in the saving function, that is suppose that in addition to  $\zeta_{it}$  the only determinant of savings is ability to learn, and consider the simple case where the previous function is linear, i.e.:

$$s_{it} = \beta \eta_{it} + \zeta_{it} \quad (12)$$

If this is the true relation between savings and ability to learn, then can we use savings to solve the endogeneity and selection problems of the OLS estimation? Yes, in fact it can be shown (see Appendix B) that the bias using the savings as a proxy variable for unobserved ability to learn can never be higher than the bias of the OLS estimates and equals:

$$E(\hat{\gamma}_1 - \gamma_1) = \frac{-\sigma_{s_t \mu} \frac{\sigma_{i s_t}}{\sigma_{i i}}}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{i s_t}^2}{\sigma_{i i}} \right]} = \frac{\sigma_{\zeta}^2}{\left[ \beta^2 \sigma_{\eta}^2 \left( 1 - r_{i \eta_{it}}^2 \right) + \sigma_{\zeta}^2 \right]} E(\hat{\gamma}_1^{OLS} - \gamma_1)$$

The extent of this bias will depend on the correlation between the regressors of interest (home and school inputs) and the proxy variable ( $\sigma_{i s_t}$ ) and the correlation between the proxy variable and the error term ( $\sigma_{s_t \mu}$ ).

To study whether the estimators are consistent we need additional information. Given that the panel gives only two saving observations per student, I will take into account two cases for the stochastic component for which I can get identification in the sample.

### 4.3.1 Identification under alternative specifications

**Measurement error** Suppose that the unobserved term  $\varsigma_{it}$  is pure measurement error. That is, assume it is *i.i.d* across individuals and time, so that  $cov(\varsigma_{it}, \varsigma_{it-1}) = 0$ . In this case we can use savings from a different period, say  $s_{i,t-1}$ , to instrument for  $s_{it}$ , as in this case  $cov(s_{i,t-1}, \varsigma_{it}) = 0$ . This procedure is called “multiple indicator solution”. To see why the bias vanishes, consider again

$$E(\hat{\gamma}_1 - \gamma_1) = \frac{-\sigma_{s_t\mu}\sigma_{\varsigma_{it}}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{\varsigma_{it}}^2]}$$

if we use  $s_{i,t-1}$  to predict  $s_{i,t}$  ( $s_{i,t} = \theta s_{i,t-1} + \xi_{it}$ ), then:

$$\sigma_{s_t\mu} = E \left[ \sum \hat{\theta} s_{i,t-1} \mu \right] = E \left[ \sum \hat{\theta} s_{i,t-1} \left( \varepsilon_{it} - \frac{1}{\beta} \zeta_{it} \right) \right]$$

where we use  $\mu_{it} = \varepsilon_{it} - \frac{1}{\beta} \zeta_{it}$  as defined in (13) Appendix B. It follows that

$$\sigma_{s_t\mu} = E \left[ \hat{\theta} \sum s_{i,t-1} \varepsilon_{it} - \frac{\hat{\theta}}{\beta} \sum s_{i,t-1} \zeta_{it} \right] = 0$$

given that  $cov(s_{i,t-1}, \varsigma_{it}) = 0$ . Which implies  $E(\hat{\gamma}_1 - \gamma_1) = 0$ .

To test the presence of measurement error in the saving function we can run the same set of regressions as in section 4.1 but instrumenting the current period saving with savings in a different period. The problem in this case is that in the estimation of Section 4.1 a fourth order polynomial expansion of parent’s savings for postsecondary education is used. That is, we have a polynomial errors-in-variables model. Identification in this case is still possible, but not by using a linear projection in the first stage. The problem is that powers of the measurement error get interacted with the coefficients, and to identified them we need to identify those moments of the error term as well. If a linear projection of the type of  $s_{i,t} = \theta s_{i,t-1} + \xi_{it}$  is used, the estimated coefficients would be a linear combination of the true coefficients and different moments of the measurement error term. Hausman, Newey, Ichimura and Powell (1991) and Hausman, Newey and Powell (1995) proposed an identification strategy for polynomial errors in variable models, and that is the one I follow in this case. To get identification, I combine a linear projection in the first stage ith moment condition between the dependent variable and the instrument, and the variable measured with error and the instrument (see the cited literature for details).

**Preference Shifter** Suppose  $\varsigma_{it}$  is persistent over time for each student, i.e.  $\varsigma_{it} = \varsigma_{it-1} = \varsigma_i$ . This scenario could arise if the unobserved component of savings is due to parents' preference parameter, like parents' generosity toward their children. In this case, instrumenting current period savings with savings in a different period would not eliminate the bias as  $cov(s_{i,t-1}, \varsigma_i) \neq 0$ . Instead the change in savings  $s_{i,t} - s_{i,t-1} = \beta(\eta_{it} - \eta_{it-1})$  does. Change in savings is correlated with savings, but not with  $\varsigma_i$  and so it allows us to get consistent estimates of our parameters of interest.

### 4.3.2 Estimation Results

Both instruments require that we observe two savings observations for each students, therefore all the estimations in this section include only the balance panel of students that do not drop out from school between 8th grade and 12th grade. Consequently I cannot estimate the survival probabilities needed to identify the coefficients in the third stage of the algorithm. To be able to run the third stage, I use each student's survival probabilities estimated from the unbalance panel. I use these probabilities for the three measures of savings: current period saving (the suggested measure), savings in a different period (measurement error case), and change in savings (preference shifter case). I reestimate the OLS coefficients for this balance panel as well.

Using the estimates of each alternative specification I compute how much of the black-white gap could be close by giving black students in the sample the average inputs white students are receiving. Table 6 presents the results under the alternative specifications, the original OLS and OP value added specifications and the two OP estimations using each instrument. In comparison with its OLS alternative, the OP estimator using current period saving does much better. The OP estimator predicts that both types of inputs, home and school, would close the gap in a smaller fraction than what OLS predicts. In both cases the OP prediction is closer to what the instrument for each extreme case predicts.

## 5 Conclusion

The existing literature on sources of inequality find that “pre-market” factors, skills individuals acquire before entering the labor market, explain most of income inequality across individuals and between groups of individuals. But what explains differences in pre-market

factors? A growing literature in economics tries to provide an answer to this question by studying children's performance in test scores . This paper contributes to that literature by proposing an identification strategy that accommodates for usual endogeneity problems in the choice of inputs and to the choice on whether to attend schools or not and applying it to a very suitable data set for this problem: NELS:88. NELS:88 provides information of both home and school inputs at the student level as well as parents' saving for their child postsecondary education that I use to control for the unobserved component (i.e. ability to learn) in the production of skills. This allows me to recover of the parameters of interest in the production function of achievement: the effect of period by period investment as well as the impact of the achievement acquired in previous periods. The estimates show that in fact the most significant change from applying the proposed strategy rather than an OLS estimation occurs in the lag test score. Additionally, I find evidence that these savings are not a poor proxy for students' unobserved ability to learn.

The estimates for the role of family inputs are in line to previous findings, they foster students achievement and there exists sensitive periods. However, the estimates of school inputs show that, contrary to what has been found in the literature, they are important for the formation of students' skills and they seem to have a higher impact if late remediation policies are considered. Therefore to correctly estimate the effect of school programs, the school inputs at the student level should be considered in the production function. I also find evidence of dynamic complementarity, i.e the higher the level of achievement students start with the higher the rate of return to that period investment.

## References

- [1] Akerberg, D, Benkard, L, Berry, S and Pakes, A (2006) “Econometric Tools for Analyzing Market Outcomes”. The Handbook of Econometrics, Heckman, J ed.
- [2] Ben-Porath, Y (1967). “The Production Function of Human Capital and the Life Cycle of Earnings” Journal of Political Economy 75: 352-365.
- [3] Blau, D and Currie, J (2006). “Pre-School, Day Care, and After-School Care: Who’s Minding the Kids?”. The Handbook of Economics of Education, Hanushek, E and Welch, F eds.
- [4] Cameron, S and Heckman, J (1998). “Life Cycle Schooling and Dynamic Selection Bias: Models and Evidence for Five Cohorts of American Males” Journal of Political Economy 106 (2).
- [5] Carneiro, P, Cunha, F and Heckman, J (2004). “The technology of Skill Formation”. Working paper, University of Chicago
- [6] Carneiro, P, Heckman, J and Masterov, D (2005). “Labor Market Discrimination and Racial Differences in Premarket Factors”. Journal of Law and Economics, Vol 48: 1-39
- [7] Cooley, J (2007). “Desegregation and the Achievement Gap: Do Diverse Peers Help?”, Working Paper, Department of Economics, University of Wisconsin-Madison.
- [8] Cunha, F (2007). “A time to plant and a time to reap”. Working paper, University of Chicago.
- [9] Cunha, F and Heckman, J. (2007a). “The Technology of Skill Formation”, American Economic Review Papers and Proceedings, forthcoming.
- [10] Cunha, F and Heckman, J. (2007b). “Formulating, Identifying, and Estimating the Technology for the Formation of Skills”. Working paper, University of Chicago.
- [11] Cunha, F, Heckman, J, Lochner, L and Masterov, D (2006) “Interpreting the Evidence on Life Cycle Skill Formation”. The Handbook of Economics of Education, Hanushek, E and Welch, F eds.

- [12] Currie, J and Thomas, D (1995). “Does Head Start Make a Difference?” *American Economic Review*, Vol. 85(3): 341-364
- [13] Currie, J and Thomas, D (2000): “School Quality and the Long-Term Effects of Head Start”. *Journal of Human Resources* 35 (4): 755-774.
- [14] Currie, J and Moretti, E (2003) “Mother’s Education and the Intergenerational Transmission of Human Capital: Evidence from College Openings”. *Quarterly Journal of Economics* 118(4): 1495-1532.
- [15] Fryer, R and Levitt, S (2004). “Understanding the Black-White Test Score Gap in the First Two Years of School”. *The Review of Economics and Statistics*, Vol. 86(2): 447-464
- [16] Greenwood, J and Seshadri, A (2005). “Technological Progress and Economic Transformation”. *Handbook of Economic Growth*, Vol 1B: 1225-1273
- [17] Hanushek, E (1986). “The Economics of Schooling: Production and Efficiency in Public Schools” *Journal of Economic Literature*, Vol. 24(3): 1141-77
- [18] Hausman, J, Newey, W, Ichimura, H and Powell, J (1991). “Identification and estimation of polynomial errors-in-variables models”. *Journal of Econometrics*, Vol 50: 273-295.
- [19] Hausman, J, Newey, W and Powell, J (1995). “Nonlinear errors in variables Estimation of some Engel curves”. *Journal of Econometrics*, Vol 65: 205-233.
- [20] Heckman, J (2000). “Policies to Foster Human Capital”. *Research in Economics* 54 (1): 3-56
- [21] Heckman, J and Rubinstein, Y. (2001). “The importance of noncognitive Skills: Lessons from the GED Testing Program”. *American Economic Review Papers and Proceedings* 91(2): 145-149.
- [22] Huggett, M, Ventura, G and Yaron, A (2007). “Sources of Lifetime Inequality” NBER Working Papers 13224
- [23] Keane, M and Wolpin, K (1997). “The Career Decisions of Young Men”. *Journal of Political Economy*, 105 (3): 473-522.

- [24] Keane, M and Wolpin, K (2001). "The Effect of Parental Transfers and Borrowing Constraints on Education Attainment". *International Economic Review* 42(4): 1051-1103.
- [25] Lee, J. (2001). *Undergraduates Enrolled with Higher Sticker Prices*. Washington, D.C., U.S. Department of Education, National Center for Education Statistics.
- [26] Levinsohn, J and Petrin, A (2003). "Estimating Production Functions Using Inputs to Control for Unobservables". *The Review of Economic Studies* 70 (2): 317-342.
- [27] Levinsohn, J, Petrin, A and Poi, B (2004). "Production Function Estimation in Stata Using Inputs to Control for Unobservables". *The Stata Journal* 4(2): 113-123.
- [28] Liu, H, Mroz, T and van der Klaauw, W (2006). "Maternal Employment, Migration and Child Development". Working paper, East Carolina University.
- [29] Neal, D and Johnson, W (1996). "The Role of Premarket Factors in Black-White Wage Differences". *Journal of Political Economy* 104 (5): 869-895.
- [30] National Center for Education Statistics.(2002) "Base-Year to Fourth Follow-up Data File User's Manual" U.S. Department of Education.
- [31] Oliver, M and Shapiro, T (2006). "Black wealth, white wealth : a new perspective on racial inequality" New York, NY.
- [32] Olley, G and Pakes, A (1996). "The Dynamics of Productivity in the Telecommunications Equipment Industry". *Econometrica* 64: 1263-1297.
- [33] Todd, P and Wolpin, K (2003). "On the Specification and Estimation of the Production Function for Cognitive Achievement". *The Economic Journal* 113 (485): F3-33.
- [34] Todd, P and Wolpin, K (2006). "The Production of Cognitive Achievement: Home, School and Racial Test Score Gaps". Working paper, University of Pennsylvania.

## 6 Appendix A: Tables

Table 1: Summary Statistics

Variable	8th Grade		12th Grade	
	Black	White	Black	White
Standardized math test score	0.300 (0.245)	0.520 (0.284)	0.290 (0.249)	0.530 (0.284)
<b>Home Inputs</b>				
Hours reading outside school	1.748 (1.719)	2.032 (1.912)	2.147 (2.118)	2.585 (2.497)
Hours of TV per week	3.499 (1.651)	2.673 (1.514)	3.209 (1.694)	2.085 (1.447)
Special lessons	0.296	0.419	0.140	0.138
<b>School Inputs</b>				
Private school	0.142	0.225	0.069	0.155
Teacher wage	9.764 (0.161)	9.730 (0.157)	9.973 (0.144)	9.946 (0.141)
Teacher experience	14.723 (7.644)	13.921 (7.540)	13.944 (10.306)	14.507 (9.168)
Teacher certified	0.478	0.503	0.630	0.645
Class enrollment	26.596 (13.096)	24.476 (11.005)	27.083 (14.935)	27.058 (17.026)
Prop. of stud receiving remedial classes	12.227 (14.091)	5.377 (7.316)	12.175 (13.576)	5.797 (7.286)
Proportion of class maintaining order	2.100 (0.853)	1.990 (0.785)	1.815 (1.019)	1.591 (0.761)
<b>Family characteristics</b>				
Mother High School	0.667	0.777	0.713	0.811
Mother Some College	0.346	0.429	0.370	0.441
Mother College	0.128	0.210	0.131	0.205
Father High School	0.357	0.642	0.367	0.672
Father Some College	0.205	0.422	0.216	0.442
Father College	0.112	0.263	0.104	0.261
Savings post secondary education	4,022 (4,138)	5,938 (5,087)	5,443 (6,830)	9,099 (9,357)
Family Income	29,729 (26,781 )	49,464 (39,993)	36,658 (32,500)	57,026 (42,512)

Table 2: Distribution of fathers' education by mothers' education

		Mother's Education		
		High School	Some College	College
Father's Education	High School	37.1%	16.4%	6.6%
	Some College	16.6%	26.2%	10.9%
	College	12.0%	28.3%	66.2%

Table 3: Regression results grade-dependent technology

	OLS	O-P estimator
Lag test score	0.5023 (0.0142)	0.6670 (0.0174)
Read in 8thG	0.0366 (0.0073)	0.0374 (0.0073)
Read in 8thG squared	-0.0030 (0.0011)	-0.0031 (0.0011)
Go to class with pencil 8thG	0.0247 (0.0109)	0.0261 (0.0110)
Special lessons 8thG	0.0246 (0.0087)	0.0244 (0.0088)
Family have books at home 8thG	0.0535 (0.0181)	0.0470 (0.0182)
Hours of TV per week 8thG	-0.0151 (0.0028)	-0.0140 (0.0028)
Time with parents 8thG	0.1308 (0.0532)	0.1496 (0.0546)
Log(teacher wage 8thG)	0.1690 (0.0319)	0.1364 (0.0328)
Teacher experience 8thG	0.0013 (0.0006)	0.0014 (0.0006)
1/(% students with single parents 8thG)	0.4230 (0.1593)	0.4657 (0.1603)
Hours of classes 8thG	0.0700 (0.0353)	0.0653 (0.0352)
Private School 8thG	0.0563 (0.0129)	0.0419 (0.0134)
1/(prop class time teacher spends maintain. Order 8thG)	0.0981 (0.0188)	0.0990 (0.0187)

Table 3 (contd.): Regression results grade-dependent technology

	OLS	O-P estimator
Read in 12thG	0.0038 (0.0024)	0.0032 (0.0024)
Go to class with pencil 12thG	0.0532 (0.0211)	0.0524 (0.0214)
Family rule about hw 12thG	0.0339 (0.0136)	0.0253 (0.0138)
Participate in community activities 12thG	0.0384 (0.0120)	0.0333 (0.0122)
No watch TV 12thG	0.0448 (0.0273)	0.0472 (0.0277)
Time with parents 12thG	0.0044 (0.0185)	-0.0022 (0.0187)
Log(teacher wage 12thG)	0.1034 (0.0409)	0.0842 (0.0422)
Private School 12thG	0.0187 (0.0163)	0.0112 (0.0170)
Teacher certified in math 12thG	0.0293 (0.0130)	0.0194 (0.0132)
1/(% students attending remedial classes)	0.0033 (0.0142)	0.0037 (0.0143)
1/(% students with single parents 12thG)	0.1747 (0.1052)	0.1918 (0.1064)
1/(prop class time teacher spends maintain. Order 12thG)	0.0868 (0.0209)	0.0652 (0.0214)
Hours of classes 12thG	-0.0074 (0.0400)	0.0213 (0.0422)

all specifications control for parents' education, race and sex

standard errors in parenthesis

Table 4: Regression results grade-dependent technology with cross effects

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Lag test score	0.4931 (0.0157)
Interaction Lag test score current inputs	1.2887 (0.5623)
Read in 8thG	0.0267 (0.0063)
Read in 8thG squared	-0.0024 (0.0008)
Go to class with pencil 8thG	0.0139 (0.0075)
Special lessons 8thG	0.0157 (0.0063)
Family have books at home 8thG	0.0156 (0.0119)
Hours of TV per week 8thG	-0.0108 (0.0026)
Time with parents 8thG	0.2882 (0.0478)
Log(teacher wage 8thG)	0.0766 (0.0246)
Teacher experience 8thG	0.0009 (0.0004)
1/(% students with single parents 8thG)	0.1966 (0.1091)
Hours of classes 8thG	-0.0031 (0.0223)
Private School 8thG	0.0258 (0.0097)
1/(prop class time teacher spends maintain. Order 8thG)	0.0560 (0.0144)

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Table 4 (Contd.): Regression results grade-dependent technology with cross effects

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Read in 12thG	0.0015 (0.0013)
Go to class with pencil 12thG	0.0425 (0.0150)
Family rule about hw 12thG	0.0120 (0.0078)
Participate in community activities 12thG	0.0180 (0.0078)
No watch TV 12thG	0.0467 (0.0183)
Time with parents 12thG	0.0084 (0.0106)
Log(teacher wage 12thG)	0.0390 (0.0246)
Private School 12thG	0.0044 (0.0092)
Teacher certified in math 12thG	0.0153 (0.0080)
1/(% students attending remedial classes)	0.0054 (0.0079)
1/(% students with single parents 12thG)	0.1050 (0.0620)
1/(prop class time teacher spends maintain. Order 12thG)	0.0370 (0.0144)
Hours of classes 12thG	0.0032 (0.0420)

---

Table 5: Accounting Exercise

OLS predicted gap	0.237
gap closed by home inputs	0.040
	16.9%
gap closed by school inputs	0.029
	12.5%
OP predicted gap	0.218
gap closed by home inputs	0.029
	13.1%
gap closed by school inputs	0.020
	9.2%
gap closed by giving inputs only in 12th grade	
home inputs	0.010
	4.7%
school inputs	0.012
	5.7%
gap closed by giving the same initial test score	0.040
	19.3%

Table 6: Robustness Analysis, accounting exercise

OLS predicted gap		0.231
	gap closed by home inputs	0.018
	gap closed by school inputs	0.020
OP current saving predicted gap		0.231
	gap closed by home inputs	0.014
	gap closed by school inputs	0.016
OP other period saving predicted gap		0.231
	gap closed by home inputs	0.011
	gap closed by school inputs	0.015
OP change in savings predicted gap		0.231
	gap closed by home inputs	0.013
	gap closed by school inputs	0.015

## 7 Appendix B: Derivation of the bias when savings are a poor proxy of ability to learn

From (12):  $\eta_{it} = (1/\beta)(s_{it} - \zeta_{it})$ , and plugging back in (11) we get:

$$\begin{aligned} h_{it} &= \gamma_0 + \gamma_1 I_{it} + \varepsilon_t + (1/\beta)(s_{it} - \zeta_{it}) \\ &= \gamma_0 + \gamma_1 I_{it} + \underbrace{\frac{1}{\beta} s_{it} - \frac{1}{\beta} \zeta_{it}}_{\mu_{it}} + \varepsilon_t \end{aligned}$$

which implies that the unobserved component equals:

$$\mu_{it} = \varepsilon_{it} - \gamma_2 \zeta_{it} = h_{it} - (\gamma_0 + \gamma_1 I_{it} + \gamma_2 s_{it}) \quad (13)$$

where  $\gamma_2 = 1/\beta$ . This model can be rewritten in deviation of the means, which results:

$$\begin{aligned} \mu_{it} &= (h_{it} - \bar{h}) - [\gamma_1 (I_{it} - \bar{I}) + \gamma_2 (s_{it} - \bar{s})] \\ &= h_{it} - [\gamma_1 i_{it} + \gamma_2 s_{it}] \end{aligned}$$

which with some abuse of notation now lower case letters refer to deviation with respect to their mean. Thus the OLS estimates in this case can be derived from:

$$\min \sum \mu_{it}^2 = \min \sum [h_{it} - (\gamma_1 i_{it} + \gamma_2 s_{it})]^2$$

The FOC are:

$$\gamma_1 : \sum_i [h_{it} - (\hat{\gamma}_1 i_{it} + \hat{\gamma}_2 s_{it})] i_{it} = 0 \quad (14)$$

$$\gamma_2 : \sum_i [h_{it} - (\hat{\gamma}_1 i_{it} + \hat{\gamma}_2 s_{it})] s_{it} = 0 \quad (15)$$

In matrix notation:

$$x_t' h_t = x_t' x_t \hat{\gamma} \quad (16)$$

where:

$$x_t' = \begin{pmatrix} i_{1t} & \dots & i_{nt} \\ s_{1t} & \dots & s_{nt} \end{pmatrix} = \begin{pmatrix} i_t \\ s_t \end{pmatrix}$$

and

$$h_t = \begin{pmatrix} h_{1,t} \\ \dots \\ h_{n,t} \end{pmatrix}$$

From the FOC (16), we get:

$$\begin{aligned}\hat{\gamma} &= (x_t'x_t)^{-1} x_t'h_t \\ \hat{\gamma} &= (x_t'x_t)^{-1} x_t'(x_t\gamma + \mu_t) \\ \hat{\gamma} - \gamma &= (x_t'x_t)^{-1} x_t'\mu_t\end{aligned}$$

Which implies that we can write the expected bias as:

$$E(\hat{\gamma} - \gamma) = E \left[ (x_t'x_t)^{-1} x_t'\mu_t \right]$$

$$E(\hat{\gamma} - \gamma) = E \left[ \begin{pmatrix} \frac{\sum s_{it}^2}{A} & \frac{-\sum i_{it}s_{it}}{A} \\ \frac{-\sum i_{it}s_{it}}{A} & \frac{\sum i_{it}^2}{A} \end{pmatrix} \begin{pmatrix} \sum i_{it}\mu_{it} \\ \sum s_{it}\mu_{it} \end{pmatrix} \right]$$

where  $A = (\sum s_{it}^2)(\sum i_{it}^2) - (\sum i_{it}s_{it})^2$ . We can re write the expected bias more compactly as:

$$\begin{aligned}E(\hat{\gamma} - \gamma) &= E \left[ \begin{pmatrix} \frac{s_{it}s_{it}}{A} & \frac{-i_{it}s_{it}}{A} \\ \frac{-i_{it}s_{it}}{A} & \frac{i_{it}i_{it}}{A} \end{pmatrix} \begin{pmatrix} i_{it}\mu_{it} \\ s_{it}\mu_{it} \end{pmatrix} \right] \\ E(\hat{\gamma} - \gamma) &= E \left[ \begin{pmatrix} \frac{s_{it}s_{it}i_{it}\mu_{it} - i_{it}s_{it}s_{it}\mu_{it}}{A} \\ \frac{-i_{it}s_{it}i_{it}\mu_{it} + i_{it}i_{it}s_{it}\mu_{it}}{A} \end{pmatrix} \right] \\ E(\hat{\gamma} - \gamma) &= \begin{pmatrix} \frac{\sigma_{i\mu}\sigma_{s_t s_t} - \sigma_{s_t\mu}\sigma_{i s_t}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{i s_t}^2]} \\ \frac{\sigma_{s\mu}\sigma_{i i_t} - \sigma_{i_t\mu}\sigma_{i s_t}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{i s_t}^2]} \end{pmatrix} \quad (17)\end{aligned}$$

Note that the OLS bias when we omit the unobserved component  $\eta_{it}$  is:

$$E(\hat{\gamma}_1^{OLS} - \gamma_1) = \frac{\sigma_{i\nu}}{\sigma_{ii}} = \frac{\sigma_{i\eta} + \sigma_{i\varepsilon}}{\sigma_{ii}} = \frac{\sigma_{i\eta}}{\sigma_{ii}}$$

Using the suggested proxy variable and assuming that all the components of the error term are orthogonal to current inputs, i.e.  $\sigma_{i\mu} = 0$ , we can re write (17) as:

$$\begin{aligned}\gamma_1 : E(\hat{\gamma}_1 - \gamma_1) &= \frac{-\sigma_{s_t\mu}\sigma_{i s_t}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{i s_t}^2]} \\ \gamma_2 : E(\hat{\gamma}_2 - \gamma_2) &= \frac{\sigma_{s_t\mu}\sigma_{ii}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{i s_t}^2]}\end{aligned}$$

In this particular example we can see that using savings as a proxy for ability provides estimates with a smaller bias than OLS, even when the relation between savings and ability is not determinist. To see this, consider the bias in  $\hat{\gamma}_1$ :

$$\gamma_1 : E(\hat{\gamma}_1 - \gamma_1) = \frac{-\sigma_{s_t\mu}\sigma_{i s_t}}{[\sigma_{ii}\sigma_{s_t s_t} - \sigma_{i s_t}^2]}$$

$$\gamma_1 : E(\hat{\gamma}_1 - \gamma_1) = \frac{-\sigma_{s_t\mu} \frac{\sigma_{ist}}{\sigma_{ii}}}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]}$$

Consider first  $\sigma_{s_t\mu}$ :

$$\sigma_{s_t\mu} = E \left[ \sum (\beta\eta_{it} + \zeta_{it}) \mu \right] = E \left[ \sum (\beta\eta_{it} + \zeta_{it}) \left( \varepsilon_{it} - \frac{1}{\beta} \zeta_{it} \right) \right]$$

$$\sigma_{s_t\mu} = E \left[ \beta \sum \eta_{it} \varepsilon_{it} + \sum \zeta_{it} \varepsilon_{it} - \sum \eta_{it} \zeta_{it} - \frac{1}{\beta} \sum \zeta_{it} \zeta_{it} \right]$$

$$\sigma_{s_t\mu} = E \left[ -\frac{1}{\beta} \sum \zeta_{it}^2 \right] = -\frac{1}{\beta} \sigma_\zeta^2$$

$\frac{\sigma_{ist}}{\sigma_{ii}}$  can be expressed in terms of the bias of the OLS estimator when we do not use savings as a proxy for unobserved ability to learn. To see this more clearly:

$$\frac{\sigma_{ist}}{\sigma_{ii}} = \frac{E \left[ \sum i (\beta\eta_{it} + \zeta_{it}) \right]}{\sigma_{ii}} = \frac{E \left[ \beta \sum i \eta_{it} \right]}{\sigma_{ii}}$$

since  $E(\eta) = 0$ ,  $E(\zeta) = 0$ , and  $\sum I \zeta_{it} = 0$  by assumption. Then

$$\frac{\sigma_{ist}}{\sigma_{ii}} = \frac{\beta \sigma_{i\eta}}{\sigma_{ii}} = \beta E(\hat{\gamma}_1^{OLS} - \gamma_1)$$

Replacing back in  $E(\hat{\gamma}_1 - \gamma_1)$ :

$$\begin{aligned} E(\hat{\gamma}_1 - \gamma_1) &= \frac{-\left(-\frac{1}{\beta} \sigma_\zeta^2\right) \frac{\beta \sigma_{i\eta}}{\sigma_{ii}}}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]} = \frac{\sigma_\zeta^2 \frac{\sigma_{i\eta}}{\sigma_{ii}}}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]} = \frac{\sigma_\zeta^2 E(\hat{\gamma}_1^{OLS} - \gamma_1)}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]} \\ &= \frac{\sigma_\zeta^2}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]} E(\hat{\gamma}_1^{OLS} - \gamma_1) \end{aligned}$$

To show that  $E(\hat{\gamma}_1 - \gamma_1) < E(\hat{\gamma}_1^{OLS} - \gamma_1)$  we need to show  $\frac{\sigma_\zeta^2}{\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]} < 1$ , or  $\sigma_\zeta^2 <$

$\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]$ . The first term of  $\left[ \sigma_{s_t s_t} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]$  can be rewritten as:

$$\begin{aligned} \sigma_{s_t s_t} &= E \left[ \sum s_{it}^2 \right] = E \left[ \sum (\beta\eta_{it} + \zeta_{it})^2 \right] \\ &= E \left[ \beta^2 \sum \eta_{it}^2 + 2\beta \sum \eta_{it} \zeta_{it} + \sum \zeta_{it}^2 \right] \\ &= \beta^2 \sigma_\eta^2 + \sigma_\zeta^2 \end{aligned}$$

where we use the fact that  $E(\eta) = E(\zeta) = 0$ . We can decompose the second term as:

$$\begin{aligned}\sigma_{ist}^2 &= E[\sum i(\beta\eta_{it} + \zeta_{it})^2] \\ &= E[\sum i\zeta_{it} + \sum i\beta\eta_{it}]^2 \\ &= E[\sum i\beta\eta_{it}]^2 = \beta^2 E(\sum i\eta_{it})^2\end{aligned}$$

This implies:

$$\begin{aligned}\sigma_{stst} - \frac{\sigma_{ist}^2}{\sigma_{ii}} &= \beta^2\sigma_\eta^2 + \sigma_\zeta^2 - \beta^2 \frac{E(\sum i\beta\eta_{it})^2}{\sigma_{ii}} \\ &= \beta^2 \left( \sigma_\eta^2 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_{ii}} \right) + \sigma_\zeta^2\end{aligned}$$

therefore, we can write the expected bias as:

$$E(\hat{\gamma}_1 - \gamma_1) = \frac{\sigma_\zeta^2}{\left[ \beta^2 \left( \sigma_\eta^2 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_{ii}} \right) + \sigma_\zeta^2 \right]} E(\hat{\gamma}_1^{OLS} - \gamma_1)$$

Then for  $\sigma_\zeta^2 < \left[ \sigma_{stst} - \frac{\sigma_{ist}^2}{\sigma_{ii}} \right]$  to hold, we need  $\beta^2 \left( \sigma_\eta^2 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_{ii}} \right) > 0$ . Note that this last condition can be written in terms of the correlation coefficient between  $\eta$  and  $i$ :

$$\begin{aligned}\beta^2 \left( \sigma_\eta^2 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_{ii}} \right) &= \beta^2 \sigma_\eta^2 \left( 1 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_\eta^2 \sigma_{ii}} \right) \\ &= \beta^2 \sigma_\eta^2 (1 - r_{i\eta_{it}}^2)\end{aligned}$$

where  $r_{i\eta_{it}}^2$  is the square of the correlation coefficient which is bounded by one. It follows that  $\beta^2 \left( \sigma_\eta^2 - \frac{\sigma_{i\eta_{it}}^2}{\sigma_{ii}} \right) > 0$  will always hold. Therefore, the bias of the contribution of inputs on the production of achievement when we use savings as a proxy for ability to learn will never exceed the bias if we ignore that proxy.

## 8 Appendix C: More Characteristics of NELS:88

NELS:88 is a nationally representative sample of eighth-graders that were first surveyed in the spring of 1988. The original sample employed a two-stage sampling design, selecting first a sample of schools and then a sample of students within these schools. In the first stage the sampling procedure set the probabilities of selection proportional to the estimated enrollment of eighth grade students. In the second stage 26 students were selected from each of those schools, 24 randomly and the other two were selected among hispanic and Asian Islander students, resulting in approximately 25,000 students. A sample of these respondents (18,221) were then resurveyed through four follow-ups in 1990, 1992, 1994, and 12,144 were interviewed again in 2000. Along with the student survey, NELS:88 included surveys of parents, teachers, and school administrators. By beginning with the 8th-grade, NELS:88 was able to capture the population of early dropouts—those who left school prior to spring term of 10th grade—as well as later dropouts (who left after spring of 10th grade). The study was designed not only to follow a cohort of students over time but also to “freshen” the sample at each of the first two follow-ups, and thus to follow multiple grade-defined cohorts over time. Thus, 10th grade and 12th grade cohorts were included in NELS:88 in the first follow-up (1990) and the second follow-up (1992), respectively. In late 1992 and early 1993, high school transcripts were collected for sample members, and, in the fall of 2000 and early 2001, postsecondary transcripts were collected, further increasing the analytic potential of the data.

Next the characteristics of each of the data collection years are summarized (See National Center for Education Statistics (2002) for a complete description):

**Base-Year Study.** The base-year survey for NELS:88 was carried out during the 1988 spring semester. The study employed a clustered, stratified national probability sample of 1,052 public and private 8th-grade schools. Almost 25,000 students across the United States participated in the base-year study. Questionnaires and cognitive tests were administered to each student in the NELS:88 base year. The student questionnaire covered school experiences, activities, attitudes, plans, selected background characteristics, and language proficiency. School principals completed a questionnaire about the school; two teachers of each student were asked to answer questions about the student, about themselves, and about their school; and one parent of each student was surveyed regarding family characteristics and student activities.

**First Follow-up Study.** Conducted in 1990, when most sample members were high school sophomores, the first follow-up included the same components as the base-year study, with the exception of the parent survey. The study frame included 19,363 in-school students, and 18,221 sample members responded. Importantly, the first follow-up study tracked base-year sample members who had dropped out of school, with 1,043 dropouts taking part in the study. Overall, the study included a total of 19,264 participating students and dropouts. In addition, 1,291 principals took part in the study, as did nearly 10,000 teachers.

**Second Follow-up Study.** The second follow-up took place early in 1992, when most sample members were in the second semester of their senior year. The study provided a culminating measurement of learning in the course of secondary school and also collected information that facilitated the investigation of the transition into the labor force and post-secondary education. The NELS:88 second follow-up resurveyed students who were identified as dropouts in 1990, and identified and surveyed additional students who had left school since the previous wave. For selected subsamples, data collection also included the sample member's parents, teachers, school administrators, and academic transcripts.

**Third Follow-up Study (NELS:88/94).** The NELS:88 third follow-up took place early in 1994. By this time in their educational careers, most of the sample members had already graduated from high school, and many had begun postsecondary education or entered the workforce. The study addressed issues of employment and postsecondary access and was designed to allow continuing trend comparisons with other NCES longitudinal studies. The sample for this follow up was created by dividing the second follow-up sample in 18 groups based on their response history, dropout status, eligibility status, school sector type, race, test score, socioeconomic status and freshened status. Each group was assigned an overall selection probability. Cases within a group were selected such that the overall probability was met, and the probability of selection within the group was proportional to each sample member second follow-up weight. The final sample size was 15,875 individuals.

**Fourth Follow-up Study (NELS:88/2000).** The fourth follow-up to NELS:88 (NELS:88/2000) included interviews with 12,144 members of the three NELS:88 sample cohorts 12 years after the base-year data collection (For costs reasons the third follow-up sample was subsample to limit the numbers of poor and difficult respondents and those who were unlikely to be located (those who couldn't be located during earlier follow-up interviews). From here 15,649

individuals were selected and 12,144 of them completed the survey). Because these data represent the period 6 years after the last contact with the sample, they will enable researchers to explore a new set of educational and social issues about the NELS:88 respondents. For example, in 2000, most of the participants from the various cohorts of NELS:88 had been out of high school for 8 years and were 26 years old. At this age, the majority of students who intend to enroll in postsecondary schools will already have done so. Thus, a large proportion of students have completed college; some completed graduate programs. Many of these young people are successful in the market place, while others have had less smooth transitions into the labor force.